Introduction to Modern Fortran

KIND, Precision and COMPLEX

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The Basic Problem

REAL must be same size as **INTEGER** This is for historical reasons – ask if you care

32 bits allows integers of up to 2147483647 Usually plenty for individual array indices

But floating-point precision is only 6 digits And its range is only $10^{-38} - 10^{+38}$

Index values are not exact in floating-point And there are many, serious numerical problems

Example

REAL, DIMENSION(2000000) :: A REAL :: X X = SIZE(A)-1 PRINT *, X

Prints 2000000.0 – which is not right That code needs only 80 MB to go wrong

See "How Computers Handle Numbers" Mainly on the numerical aspects

Ordinary REAL Constants

These will often do what you expect

But they will very often lose precision

0.0, 7.0, 0.25, 1.23, 1.23E12, 0.1, 1.0E-1, 3.141592653589793

Only the first three will do what you expect

• In old Fortran constructs, can cause chaos E.g. as arguments to external libraries

KIND Values

You can get the KIND of any expression

KIND(var) is the KIND value of var KIND(0.0) is the KIND value of REAL KIND(0.0D0) is that of DOUBLE PRECISION This is described in a moment

Implementation-dependent integer values selecting the type (e.g. a specific REAL)

Don't use integer constants directly

SELECTED_REAL_KIND

You can request a minimum precision and range Both are specified in decimal

SELECTED_REAL_KIND (Prec [, Range])

This gives at least Prec decimal places and range $10^{-Range} - 10^{+Range}$

E.g. SELECTED_REAL_KIND(12) at least 12 decimal places

Warning: Time Warp

Unfortunately, we need to define a module We shall cover those quite a lot later

The one we shall define is trivial Just use it, and don't worry about the details Everything you need to know will be explained

Just compile it, but don't link it, using –c nagfor –C=all –c double.f90

Using KIND (1)

You should write and compile a module

MODULE double INTEGER, PARAMETER :: DP = & SELECTED_REAL_KIND(12) END MODULE double

Immediately after every procedure statement I.e. PROGRAM, SUBROUTINE or FUNCTION

USE double IMPLICIT NONE

Using KIND (2)

Declaring variables etc. is easy

REAL(KIND=DP) :: a, b, c REAL(KIND=DP), DIMENSION(10) :: x, y, z

Using constants is more tedious, but easy

0.0_DP, 7.0_DP, 0.25_DP, 1.23_DP, 1.23E12_DP, 0.1_DP, 1.0E-1_DP, 3.141592653589793_DP

That's really all you need to know . . .

Using KIND (3)

Note that the above makes it trivial to change ALL you need is to change the module

MODULE double INTEGER, PARAMETER :: DP = & SELECTED_REAL_KIND(15, 300) END MODULE double

(15, 300) requires IEEE 754 double or better

Or even: SELECTED_REAL_KIND(25, 1000)

DOUBLE PRECISION (1)

• The best way to control precision Most flexible, portable and future-proof Advisable if you may want to use HECToR

All older (Fortran 77) code will do it differently And quite a lot of programmers still do The old method is fairly reliable, today

• You need to know about this, but avoid it

DOUBLE PRECISION (2)

DOUBLE PRECISION takes the space of 2 REALs
⇒ It need not be any more accurate, though

• Almost always, REAL is 32-bit IEEE 754 And DOUBLE PRECISION is 64-bit IEEE 754 Precision is 15 digits, range is $10^{-300} - 10^{+300}$

Main exception is Cray vector supercomputers And when using compiler options to change precision

DOUBLE PRECISION (3)

You can use it just like **REAL** in declarations Using **KIND** is more modern and compact

REAL(KIND=KIND(0.0D0)) :: a, b, c

Constants use D for the exponent – 1.23D12 or 0.0D0

REAL(KIND=KIND(0.0D0)) :: a, b, c DOUBLE PRECISION, DIMENSION(10) :: x, y, z

0.0D0, 7.0D0, 0.25D0, 1.23D0, 1.23D12, 0.1D0, 1.0D-1, 3.141592653589793D0

Intrinsic Procedures

Almost all intrinsics 'just work' (i.e. are generic) IMPLICIT NONE removes most common traps

- Avoid specific (old) names for procedures AMAX0, DMIN1, DSQRT, FLOAT, IFIX etc.
- **DPROD** is also not generic use a library
- Don't use the **INTRINSIC** statement
- Don't pass intrinsic functions as arguments

Type Conversion (1)

This is the main "gotcha" – you should use

REAL(KIND=DP) :: x x = REAL(<integer expression>, KIND=DP)

Omitting the KIND=DP may lose precision

With no warning from the compiler

Automatic conversion is actually safer!

x = <integer expression>
x = SQRT(<integer expression>+0.0_DP)

Type Conversion (2)

There is a legacy intrinsic function If you are using explicit DOUBLE PRECISION

x = DBLE(<integer expression>)

All other "gotchas" are for COMPLEX

Warning

You will often see code like: REAL*8 X, Y, Z INTEGER*8 M, N

Most of the Web and many books are wrong

A Fortran IV feature, NOT a standard one '8' is NOT always the size in bytes

I strongly recommend converting to KIND

Old Fortran Libraries

Be very careful with external libraries

• Make sure argument types are right Automatic conversion does not happen Not will you get a diagnostic (in general)

Any procedure with no explicit interface I did say that using old Fortran was more painful

INTEGER KIND

You can choose different sizes of integer

INTEGER, PARAMETER :: big = & SELECTED_INT_KIND(12) INTEGER(KIND=big) :: bignum

bignum can hold values of up to at least 10^{12} Few users will need this – mainly for OpenMP

Some compilers may allocate smaller integers E.g. by using SELECTED_INT_KIND(4)

CHARACTER KIND

It can be used to select the encoding It is mainly a Fortran 2003 feature

Can select default, ASCII or ISO 10646 ISO 10646 is effectively Unicode Useful for handling non-ASCII character sets

It is not covered in this course Very few scientists want or use it

Complex Arithmetic

Fortran is the answer – what was the question?

Has always been supported, and well integrated

COMPLEX is a (real, imaginary) pair of REAL It uses the same KIND as underlying reals

COMPLEX(KIND=DP) :: c c = (1.23_DP,4.56_DP)

Full range of operations, intrinsic functions etc.

Example

COMPLEX(KIND=DP) :: c, d, e, f

 $c = (1.23_DP, 4.56_DP)*CONJG(d)+SIN(f*g)$ e = EXP(d+c/f)*ABS(LOG(e))

The functions are the complex forms E.g. ABS is $\sqrt{re^2 + im^2}$ CONJG is complex conjugate, of course

Using COMPLEX really IS that simple!

Worst "Gotcha"

Must specify KIND in conversion function

c = CMPLX(<X-expr>, KIND=DP)
c = CMPLX(<X-expr>, <Y-expr>, KIND=DP)

This will not work – KIND is default REAL Usually with no warning from the compiler

 $c = CMPLX(0.1_DP, 0.2_DP)$

Conversion to REAL

REAL(KIND=DP) :: x
COMPLEX(KIND=DP) :: c
...lots of statements ...
X = X+C
c = 2.0_DP*x

Loses the imaginary part, without warning Almost all modern languages do the same

A Warning for Old Code

 $C = DCMPLX(0.1_DP, 0.1_DP)$

That is often seen in Fortran IV legacy code It doesn't work in standard (modern) Fortran

• It will be caught by IMPLICIT NONE

Complex I/O

The form of I/O we have used is list-directed COMPLEX does what you would expect

COMPLEX(KIND=DP) :: c = (1.23_DP,4.56_DP) WRITE (*, *) C

Prints "(1.23,4.56)" And similarly for input

There is some more on COMPLEX I/O later

Exceptions

Complex exceptions are mathematically hard
Overflow often does what you won't expect Fortran, unfortunately, is no exception to this

See "How Computers Handle Numbers"

- Don't cause them in the first place
- Use the techniques described to detect them